



# A COMPLETE SCHEME OF IONIZATION COOLING FOR A MUON COLLIDER

Robert B. Palmer, J. Scott Berg, Richard C. Fernow, Juan C.  
Gallardo (BNL)

Yuri Alexahin, David Neuffer (FNAL)

D. Summers (Mississippi University)

Stephen A. Kahn (Muons Inc.)

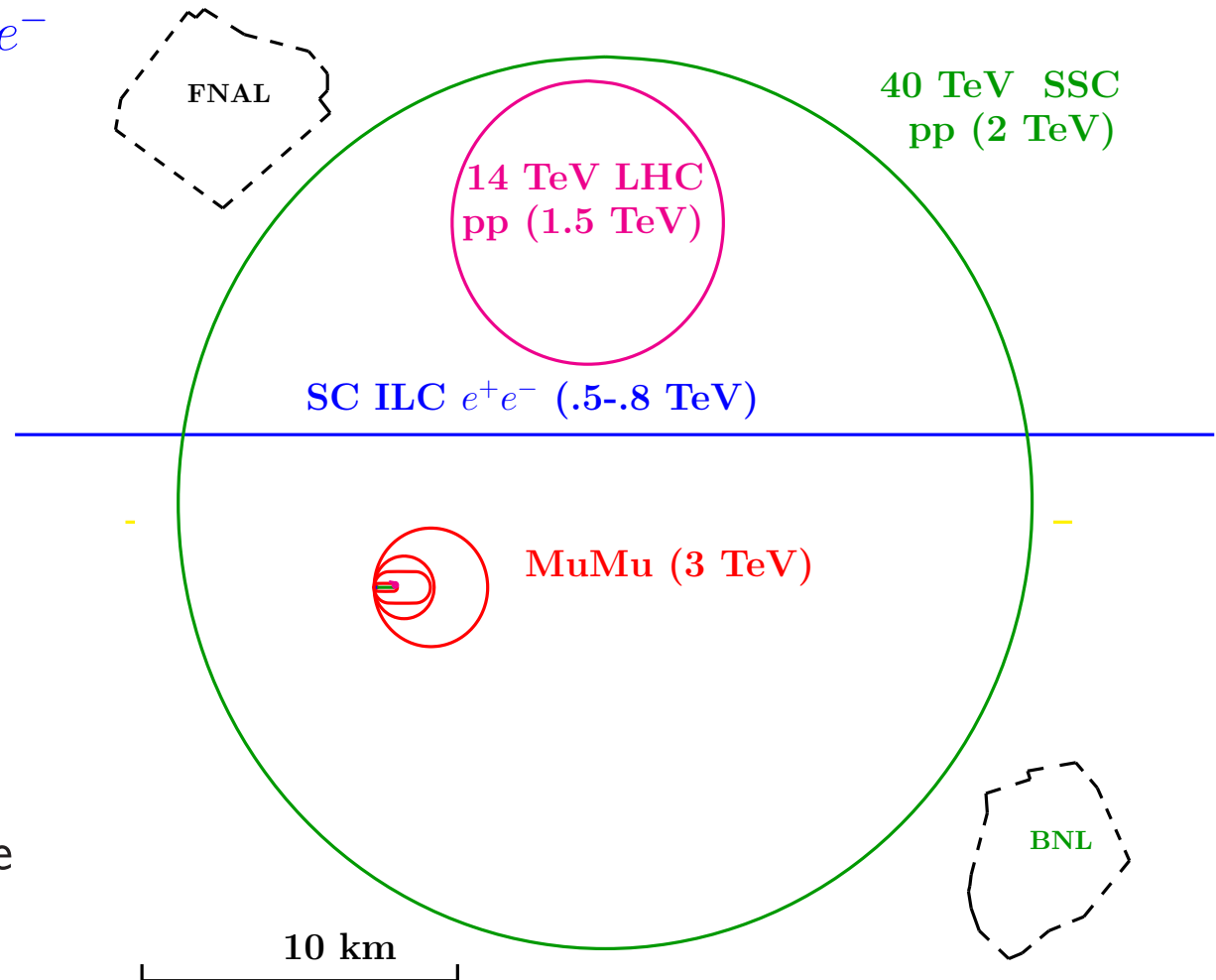
(RHIC Users June 20 2007)

## History

1969	Concept discussed	Budker
1981	Muon Ionization Cooling	Skrinsky, Parkhomchuk
1983	First outline	Neuffer
1994	Solenoid capture	Palmer
1996	Snowmass Feasibility Study	
1997	US Collaboration Formed	
1998	DoE organization and funding	
2006	Muon Collider Task Force	FNAL
2007	First Complete Scenario with simulations	This paper

# Why a Muon Collider?

- Point like interactions as in  $e^+e^-$
- Negligible synchrotron radiation:  
Acceleration in rings vs. linear  $e^+e^-$   
Small footprint
- Collider is a Ring  
 $\approx 1000$  interactions per bunch  
Larger spot for same luminosity  
Easier tolerances
- Negligible Beamstrahlung  
Narrow energy spread
- 40,000 greater S channel Higgs  
Study widths  
**BUT**
- Muons from pion decay are diffuse  
Need cooling
- Muons decay  
No time for ordinary cooling  
Acceleration must be rapid



# Luminosity Dependence

$$\mathcal{L} \propto n_{\text{turns}} f_{\text{bunch}} \frac{N_{\mu}^2}{\sigma_{\perp}^2} \quad \Delta\nu \propto \frac{N_{\mu}}{\epsilon_{\perp}}$$

$$\mathcal{L} \propto B_{\text{ring}} P_{\text{beam}} \Delta\nu \frac{1}{\beta^*}$$

- Higher  $\mathcal{L}/P_{\text{beam}}$  requires lower  $\beta_{\perp}$  or correction of  $\Delta\nu$
- Lower emittances do not directly improve Luminosity/Power
- Why do we want "Low Transverse Emittance ?
  - To reduce aberrations in Ring IP to allow lower  $\beta^*$
- Why do we want "Low Longitudinal Emittance ?
  - To reduce  $dp/p$  & chromatic aberrations in Ring IP to allow lower  $\beta_{\perp}$
  - To keep  $\sigma_z < \beta_{\perp}$  as  $\beta^*$  is reduced

# Collider Parameters

	This Paper	Snowmass	Extrapolation	
C of m Energy	1.5	4	8	TeV
Luminosity	1	4	8	$10^{34} \text{ cm}^2 \text{ sec}^{-1}$
Beam-beam Tune Shift	0.1	0.1	0.1	
Muons/bunch	2	2	2	$10^{12}$
Ring <bending field>	5.2	5.18	10.36	T
Ring circumference	3	8.1	8.1	km
Beta at IP = $\sigma_z$	10	3	3	mm
rms momentum spread	0.09	0.12	0.06	%
Muon Beam Power	7.5	9	9	MW
Required depth for $\nu$ rad	$\approx 135$	135	540	m
Efficiency $N_\mu/N_{\mu 0}$	0.07	0.07	0.07	
Repetition Rate	12	6	3	Hz
Proton Driver power	$\approx 4$	$\approx 1.8$	$\approx 0.8$	MW
Trans Emittance	25	25	25	pi mm mrad
Long Emittance	72,000	72,000	72,000	pi mm mrad

- Emittance and bunch intensity requirement same for all examples  
Because beam-beam tune shift is independent of energy

# Proton Driver

- Average proton power of 4 MW
- Protons per bunch  $8 \cdot 10^{13}$  at 24 GeV
- Extracted bunches must have  $\sigma_t \leq 3$  (nsec)

These are tough requirements    Possible parameters might be:

Proton Energy	(GeV)	12	25	50
Protons accelerated	$10^{14}$	5	5	5
Protons/bunch	$10^{14}$	1.6	0.8	0.4
Bunches extracted		3	6	12
Repetition rate	(Hz)	4	2	1

- Achieving the 3 nsec bunches at less than 25 GeV would appear hard
- Higher repetition rate and fewer protons per cycle is an option
- Higher cooling efficiency could ease these requirements
- Needs more study

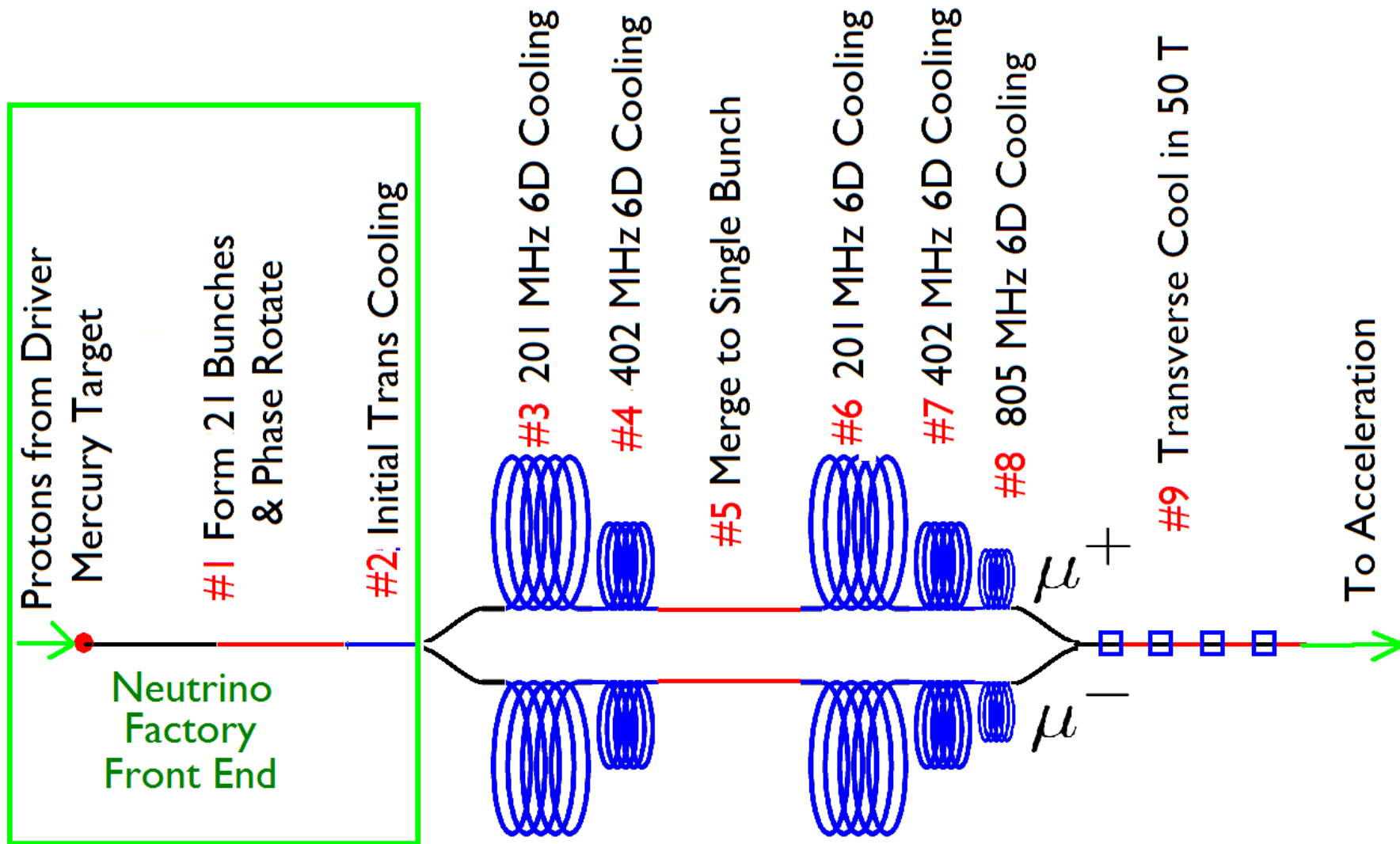
# Capture and Cooling Scheme

Essential Elements of this Solution:

- Target an intense short proton bunch on a liquid metal target  
Any other target would break
- Capture pions with high field solenoid ( $\approx 20$  T)  
Collects 50% of all useful pions of both signs
- Phase rotation into multiple bunches at moderate frequency (201 MHz)
- Ionization cooling to cool rapidly in transverse directions
- Emittance Exchange using dispersion and wedges to cool longitudinally
- Bunch merging after initial 6D cooling  
To get single intense bunches
- Re-cooling after merge  
to get single intense cold bunches

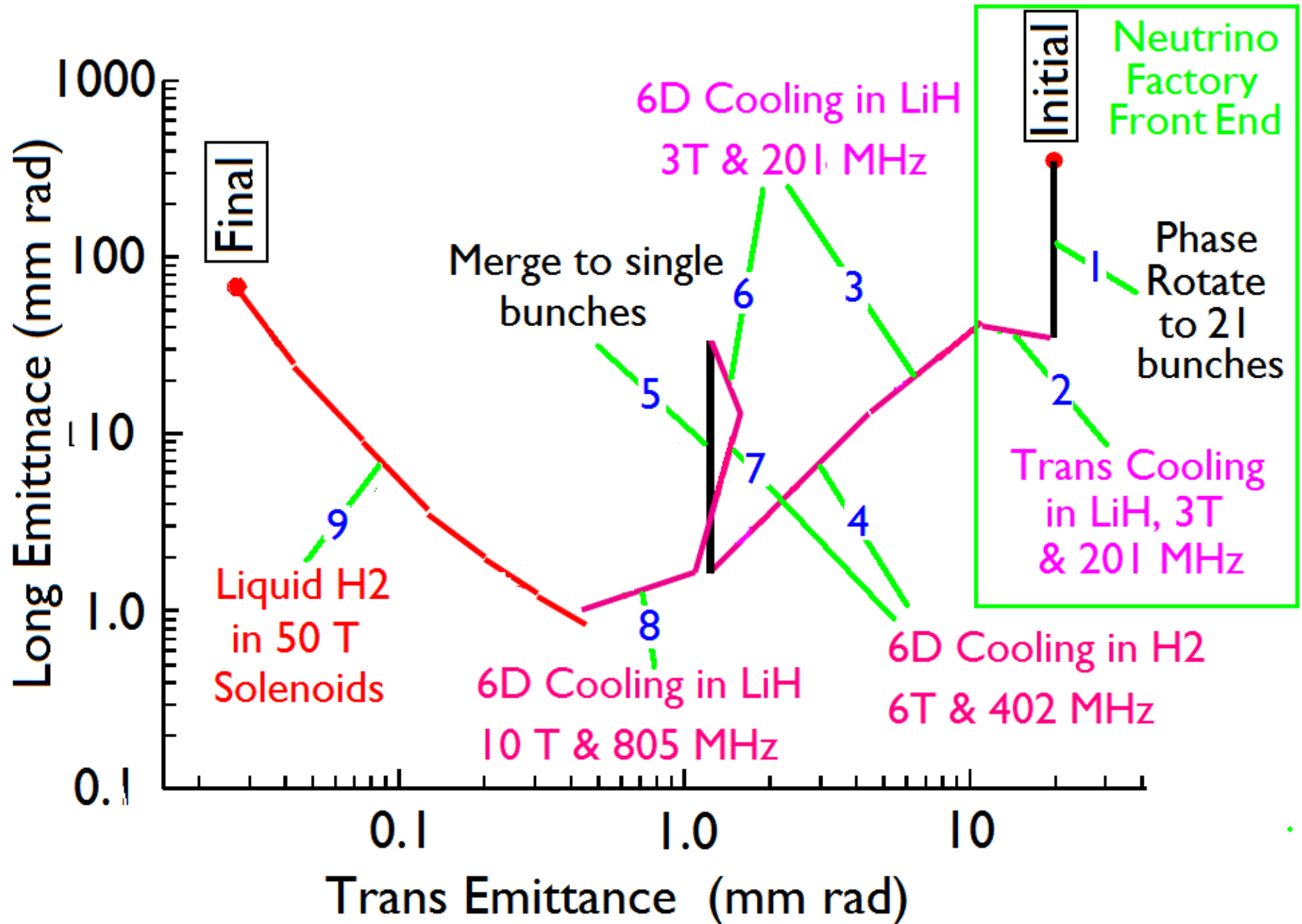
Without any one of these elements, we cannot achieve the requirements

# Capture and Cooling Schematic



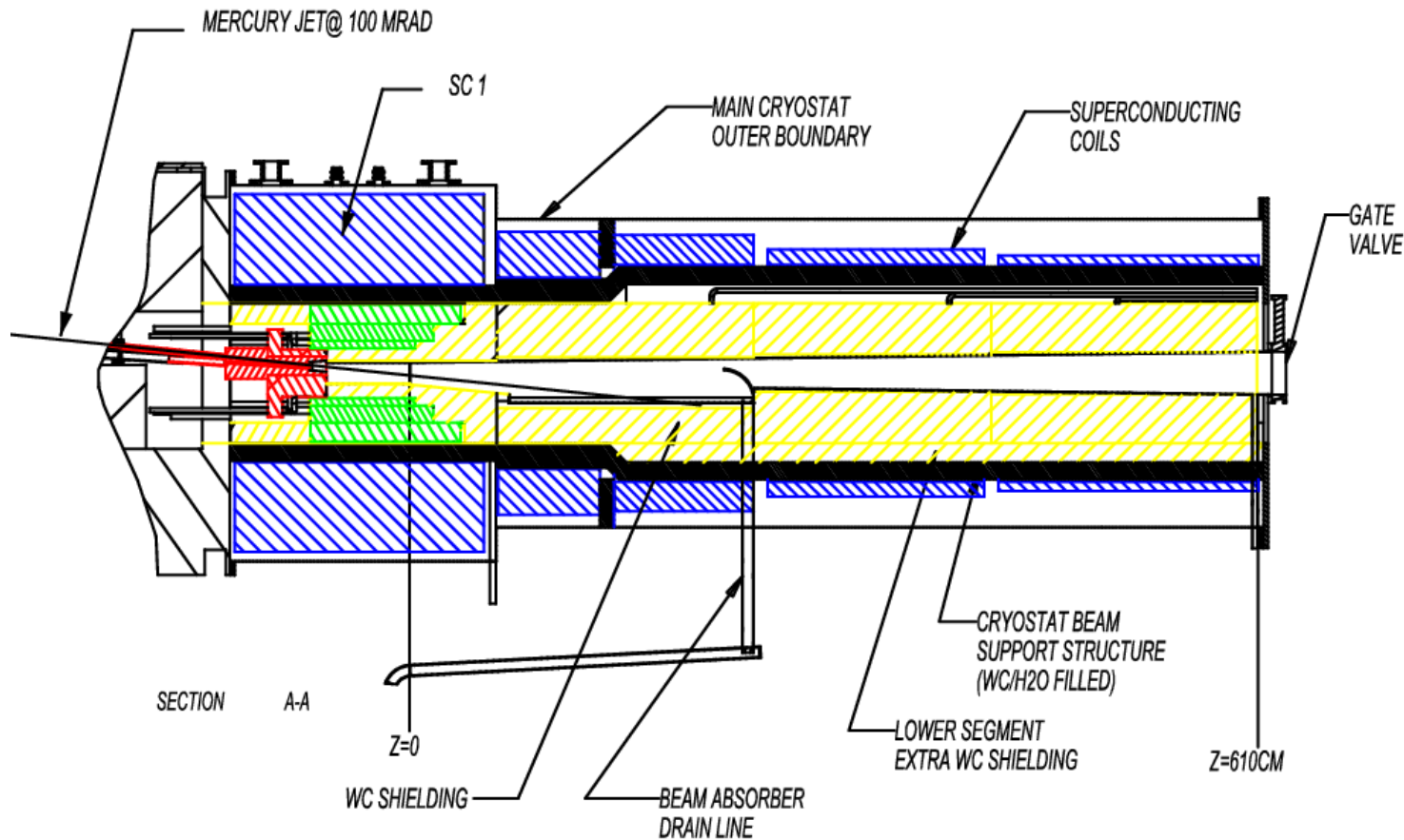
- Not to scale overall length of order 1 km
- We will look at each numbered component later

# Emittances vs. Stage





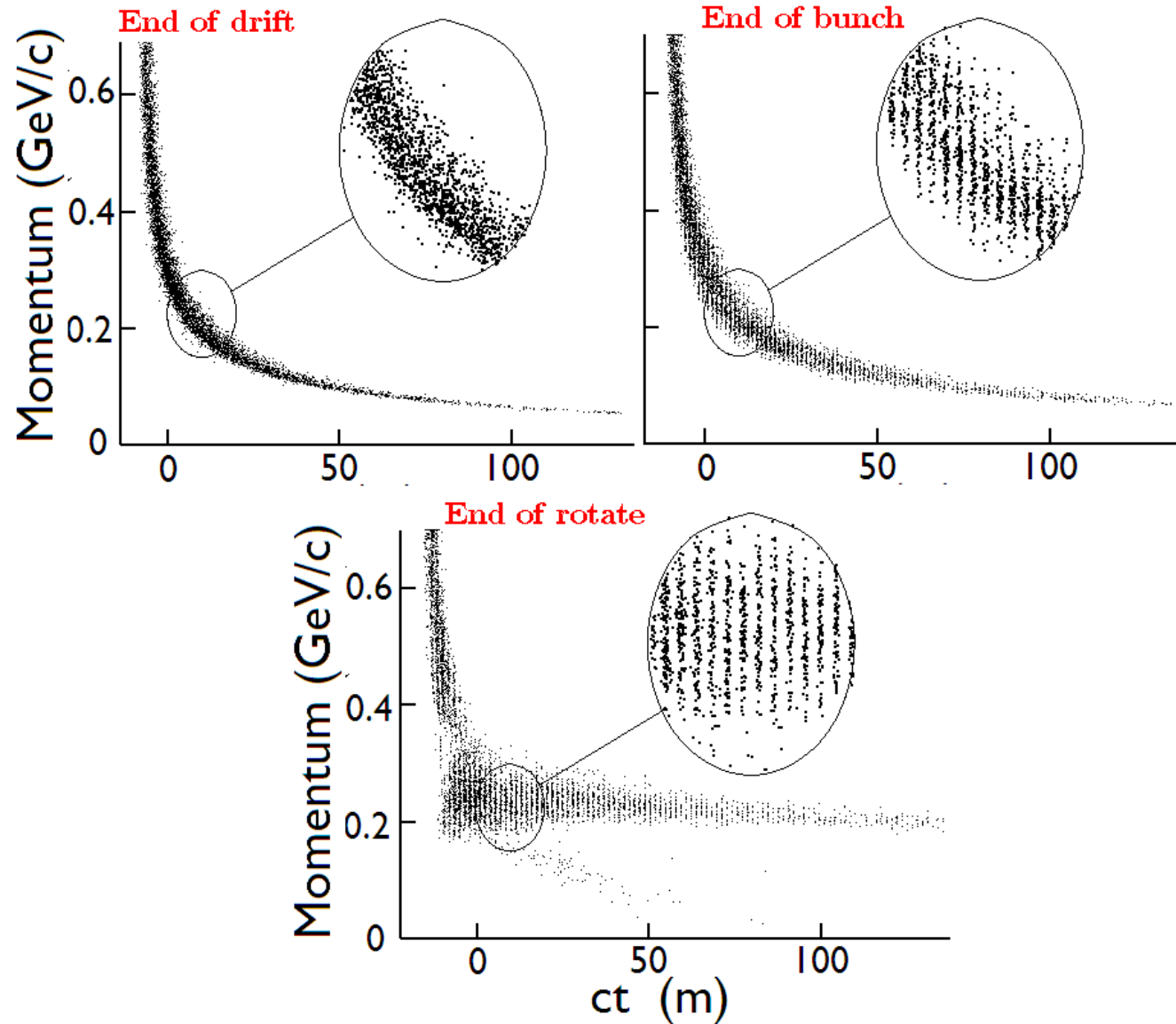
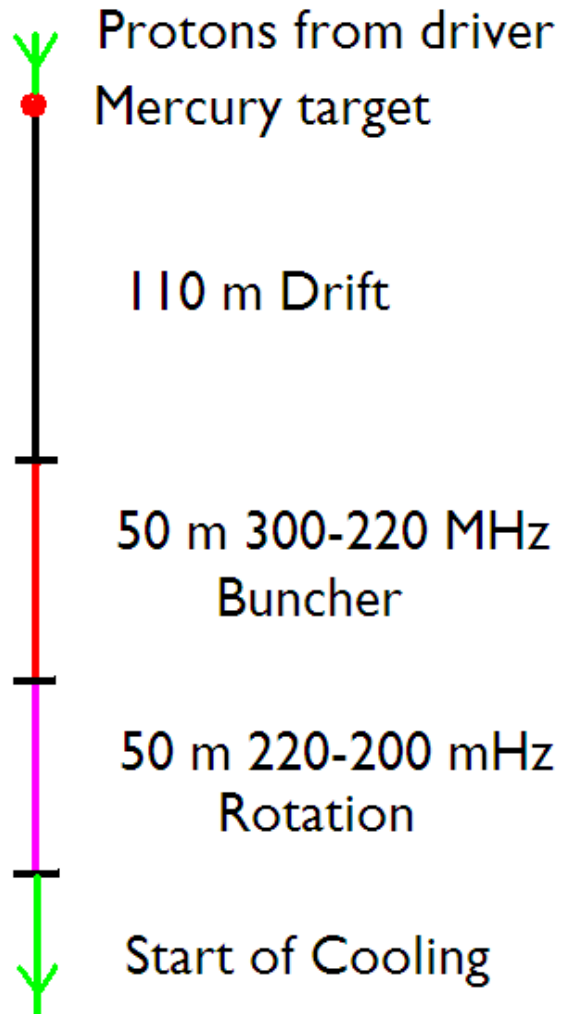
# #1 Target and Capture and Phase Rotate



- Liquid mercury Jet 'destroyed' on every pulse
- 20 T Solenoid captures all low momentum pions
- Field subsequently tapers down to approx 2 T
- Target tilted to maximize extraction of pions
- MERIT Experiment at CERN will test this concept

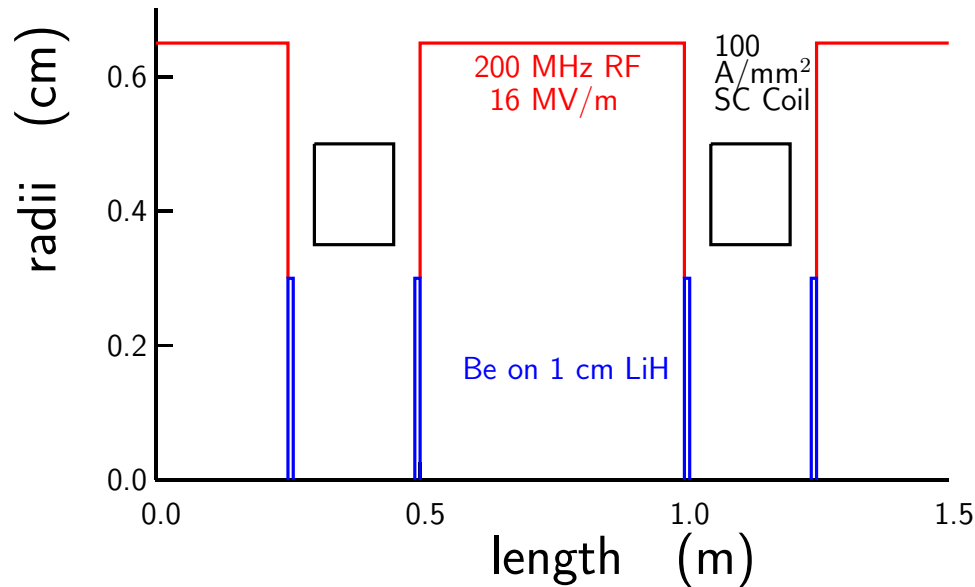
# Phase Rotation Simulation

capture into multi-bunches to reduce momentum spread

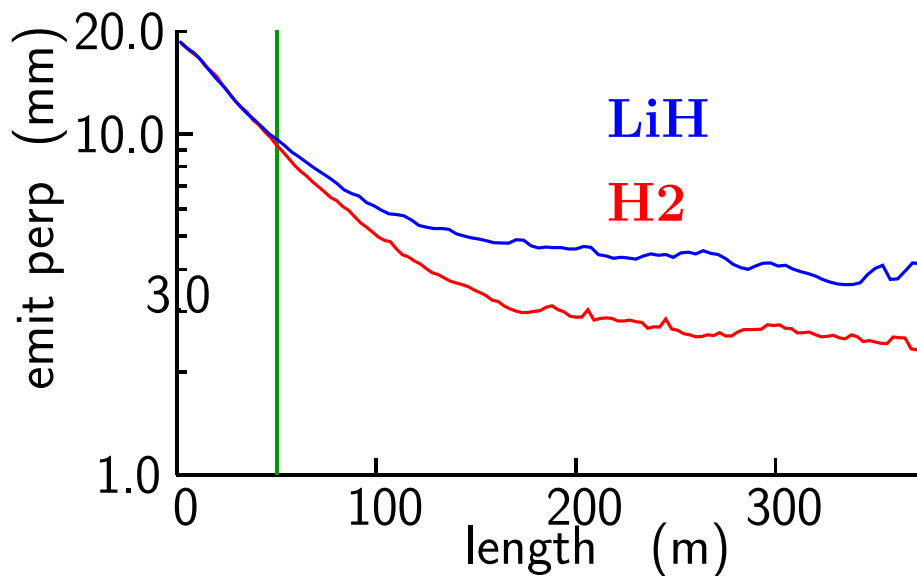


## #2 Initial Linear cooling

Only Ionization cooling is fast enough



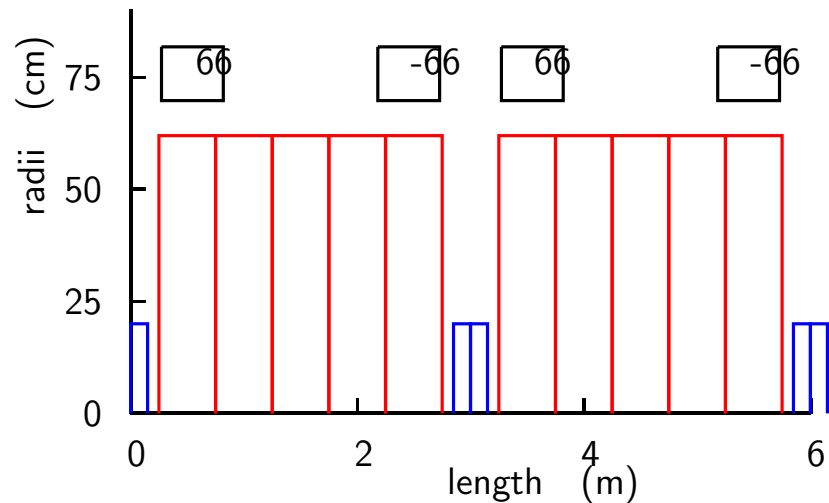
- Linear channel cools both signs transversely
- Tapering the focus field should improve performance  
(not yet assumed)



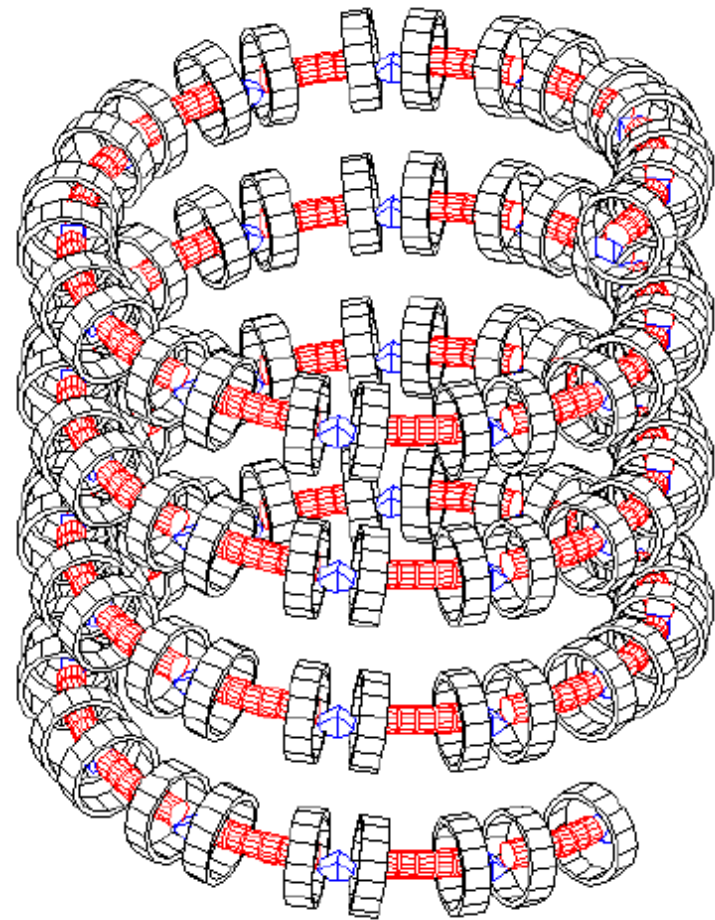
- Negligible difference between LiH and H<sub>2</sub> before 50 m
- MICE Experiment at RAL will demonstrate Ionization Cooling

## #3 #4 6D Cooling in Guggenheim helices

- RFOFO lattices
- Bending gives dispersion
- Wedge absorbers give emittance exchange → Cooling also in longitudinal
- Use as 'Guggenheim' helix
  - Because bunch train fills ring
  - Avoids difficult kickers
  - Better performance possible by tapering (Not yet assumed)



RFOFO Lattice

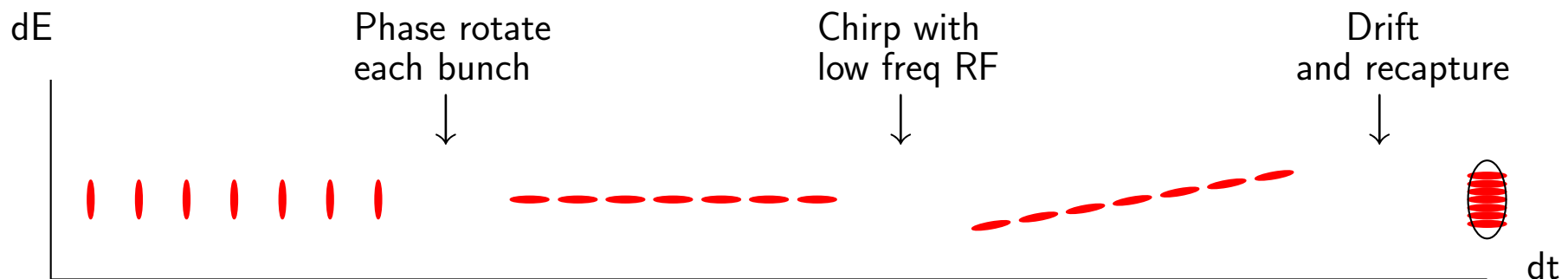


'Guggenheim'

## #5 Bunch Merging

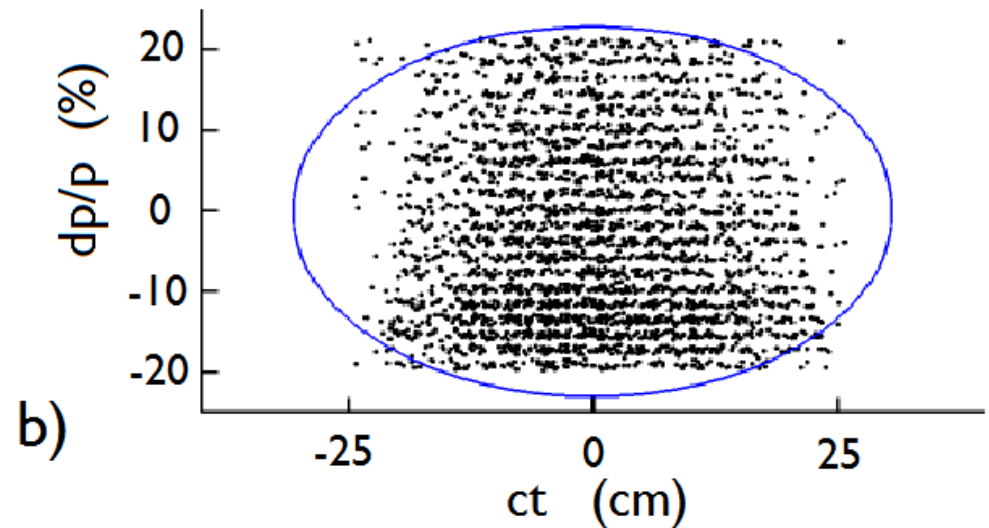
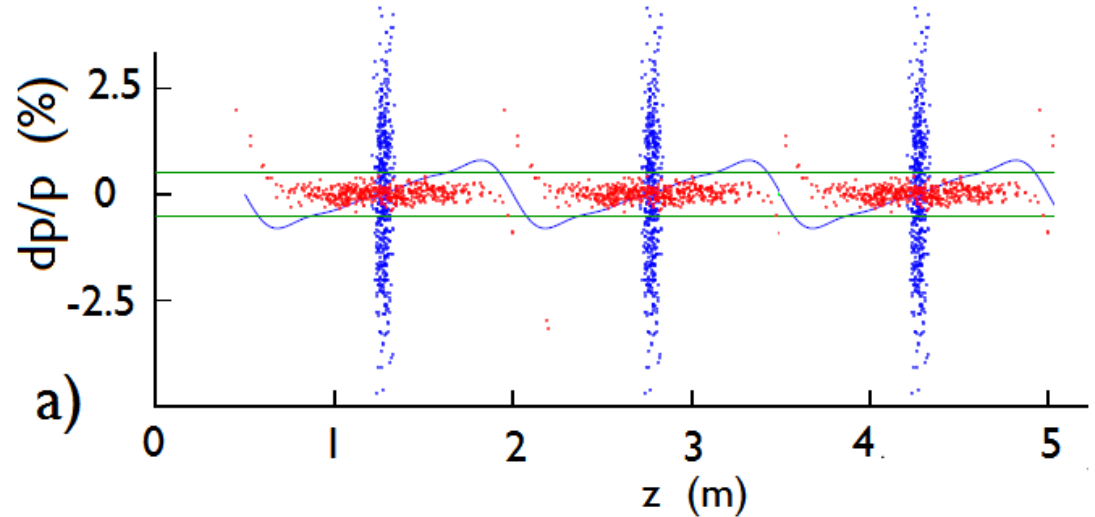
- Luminosity proportional to muons per bunch squared
- Few large bunches required
- Capturing to one large bunch would have required low frequency rf ( $\approx 30$  MHz) with low gradients and inefficiency
- We thus:
  - Capture into multiple bunches at 201 MHz
  - Cool them till small enough to:
  - Merge them and recapture at 201 MHz
  - Re-cool the merged bunches

## Merging Scheme



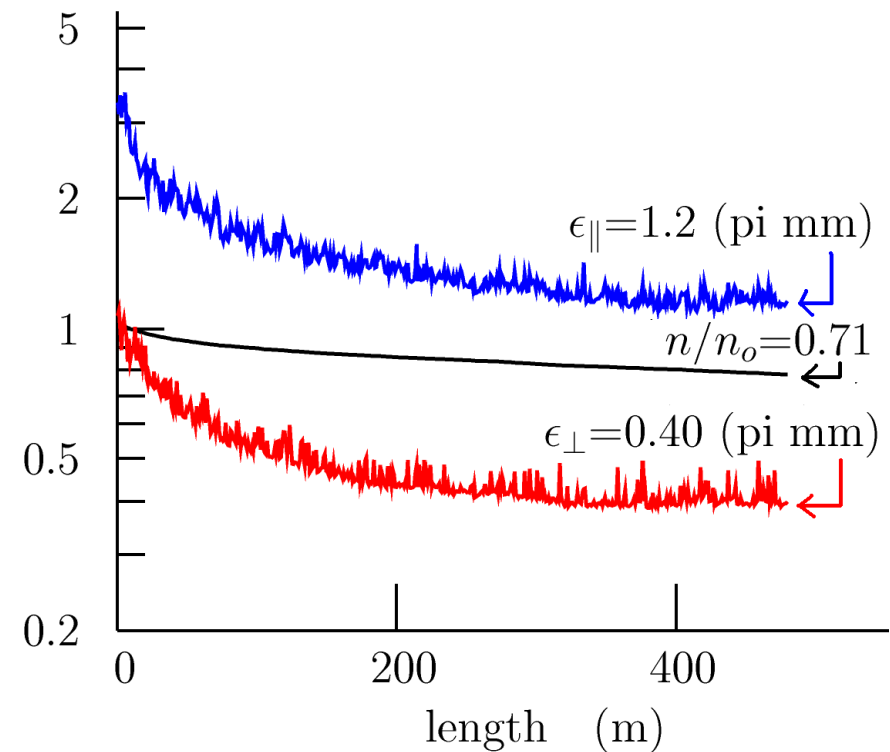
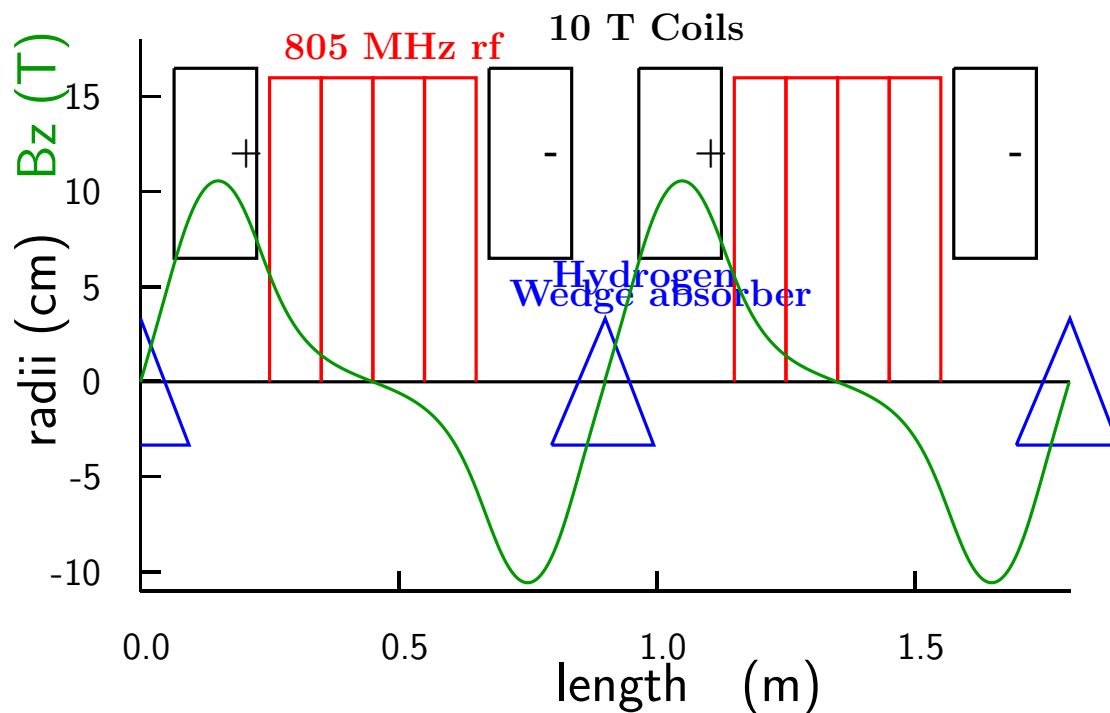
# Bunch Merging Simulation

- Drifts in 1 T wigglers, simulated in ICOOL vs amp and mom
- rf:
  - 1) at 200 MHz + 2 harmonics
  - 2) at 5 MHz + 2 harmonicsSimulated off line with parameters from ICOOL



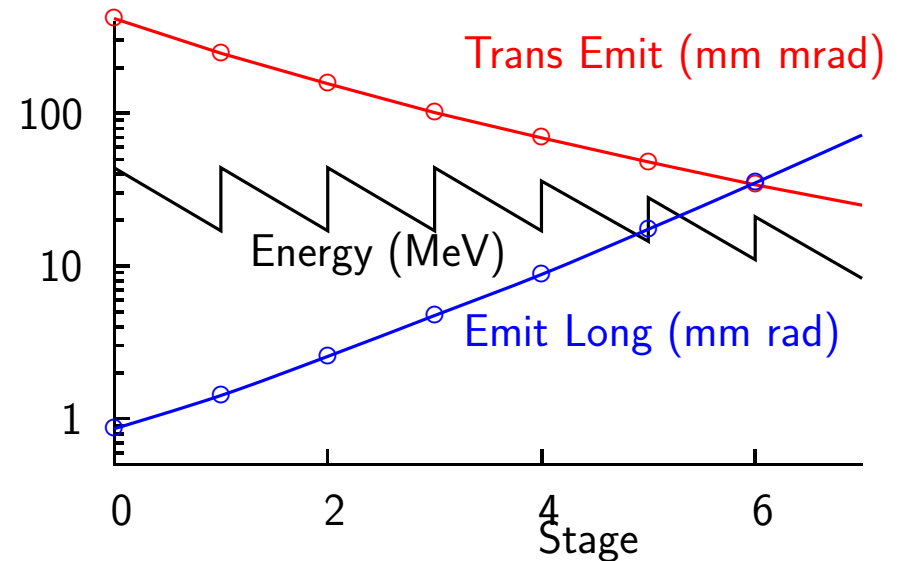
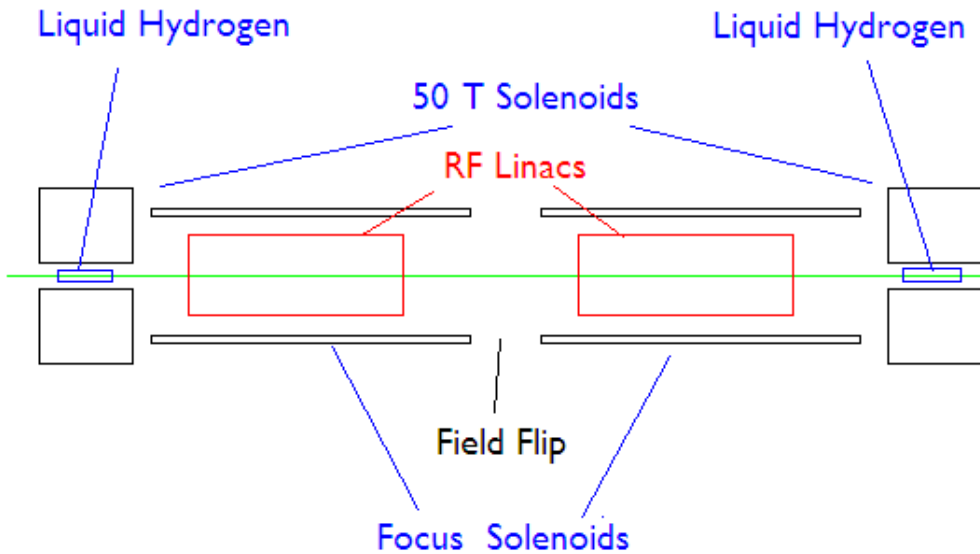
# Cooling after merge

- #6 #7 Re-cooling in Guggenheim Lattices
  - Essentially identical to #3 and #4
  - Could re-use #3 and #4
- #8 Last 6D cooling in higher field lattice
  - Uses 10 T high current density ( $150 \text{ A/mm}^2$ ) solenoids



## #9 Transverse Cooling in Very High Field Solenoids

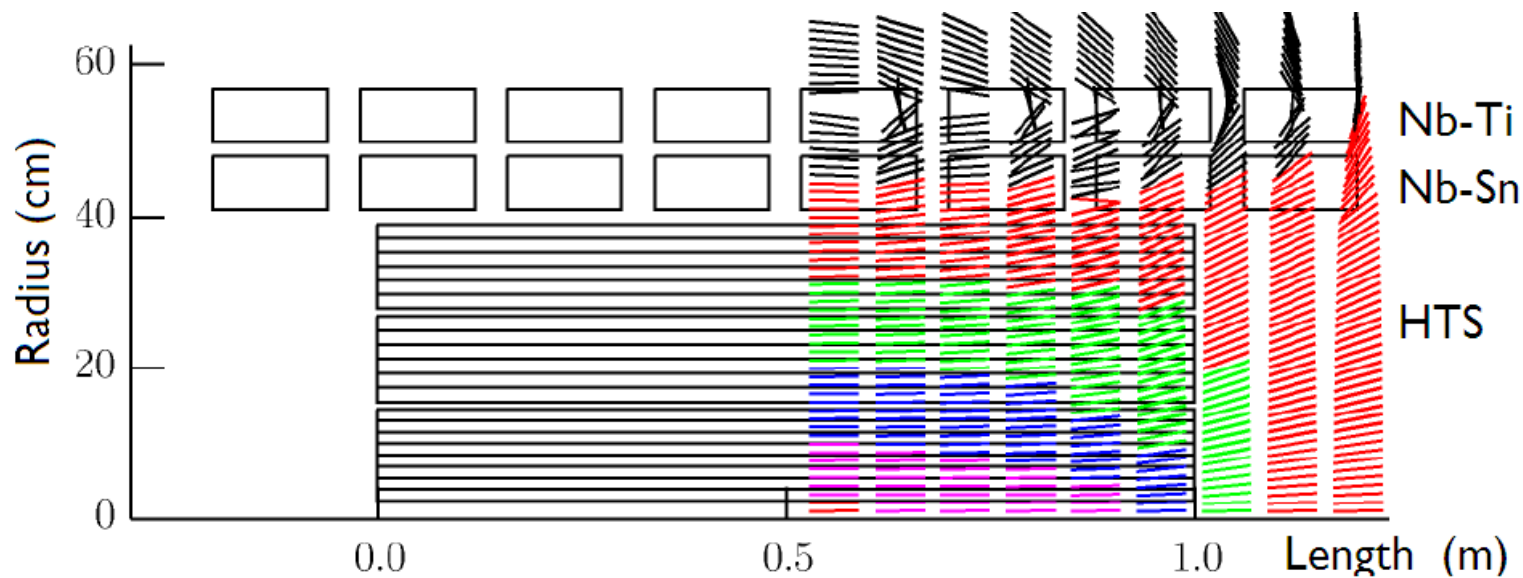
- Lower momenta allow strong transverse cooling, but long emittance rises:
- Effectively reverse emittance exchange



- 50 T HTS Solenoids
  - Layer wound allowing current to vary with radius
  - Vary ss support with radius to keep strain constant
  - Existing HTS tape at 4.2 deg. gave 50 T with rad=57 cm
- 7 solenoids with liquid hydrogen
- ICOL Simulation ( Ideal Matching and reacceleration, Transmission 97% )

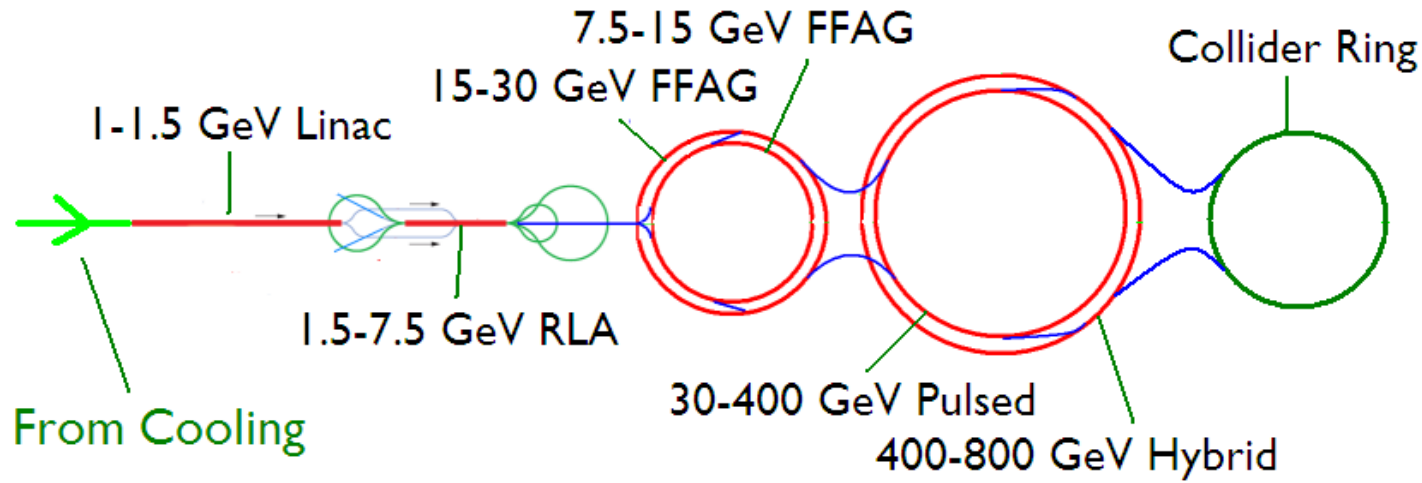


## Details of 50 T Solenoid

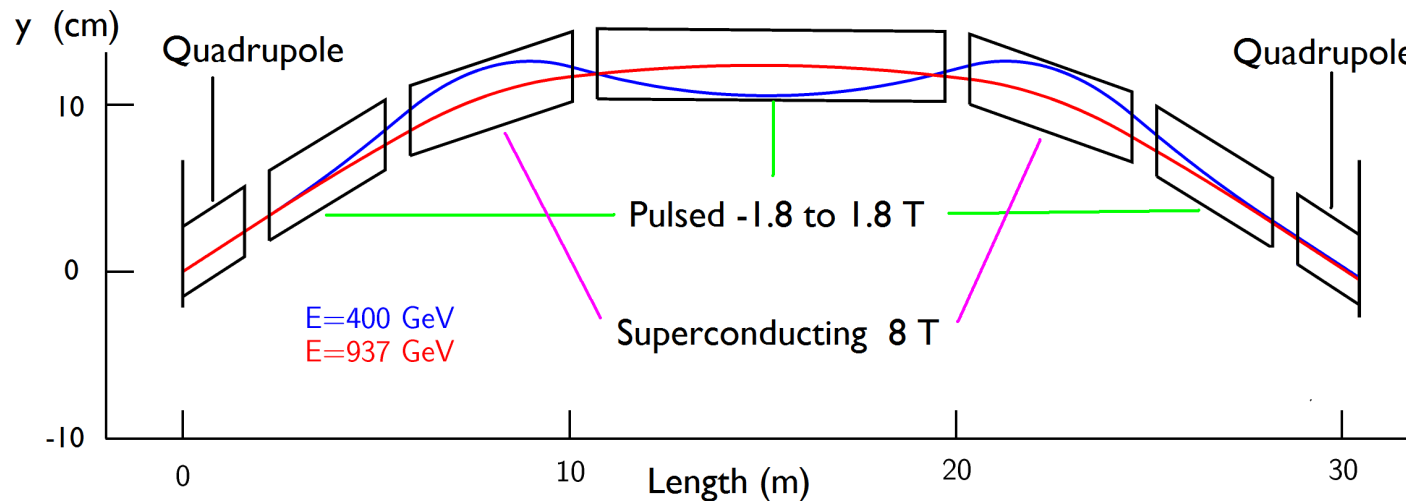


- Design uses BSCCO tape (conductor cost now 2.7 M\$, but falling)
- Stored energy 141 MJ (requires multiple local quench protections)
- Questions raised about stress cycling in BSCCO
- YBCO claimed to be much better, but more sensitive to field directions
- Needs characterizations of materials
- Highest field HTS now under construction is only 30 T
- Another case of HEP pushing SC technology

# Acceleration



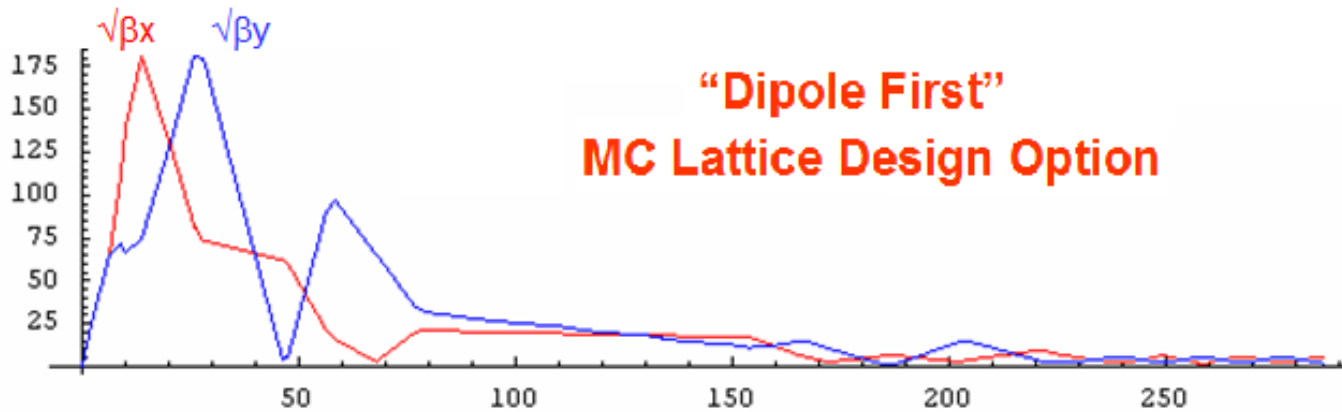
- Hybrid SC and pulsed synchrotron 400-750(930) GeV (in Tevatron tunnel)



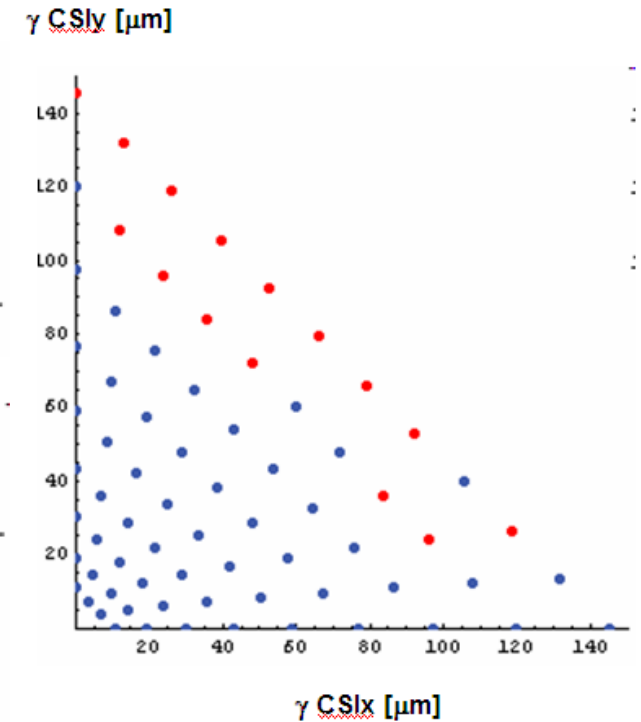
- All RLAs with ILC cavities is an alternative but more expensive

# Collider Ring (Y. Alexahin E. Gianfelice-Wendt)

## “Dipole First” MC Lattice Design Option



Lattice

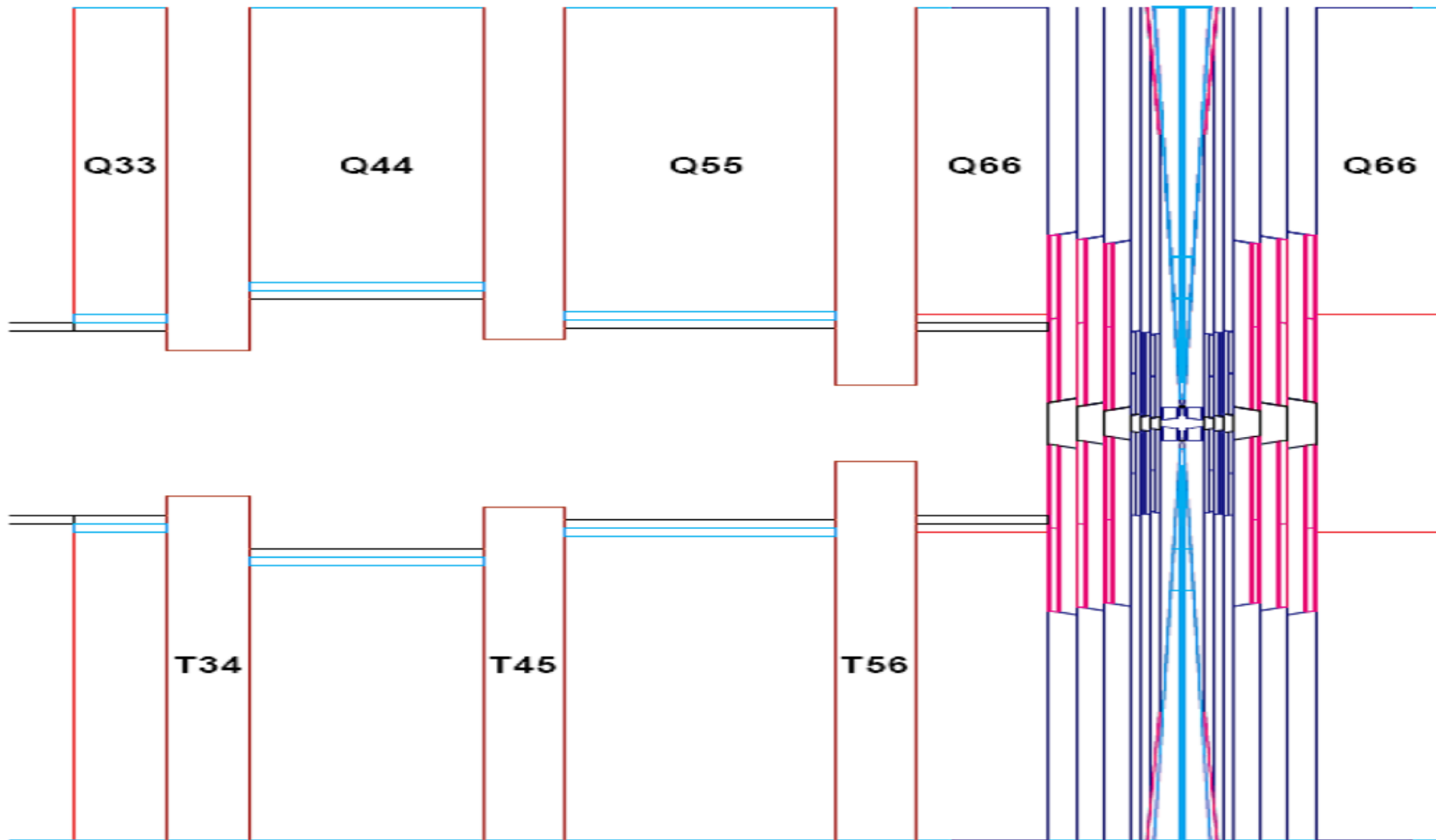


Acceptance

- $\beta^* = 1cm$   $\Delta p/p \approx 0.6 \%$   
More than adequate for rms  $dp/p=0.09 \%$
- $\Delta x, y \approx 2\sigma$  at 25 mm mrad emittance  
Will require scraping of beam (cut at 1.75 sigma loses only 5% of luminosity)

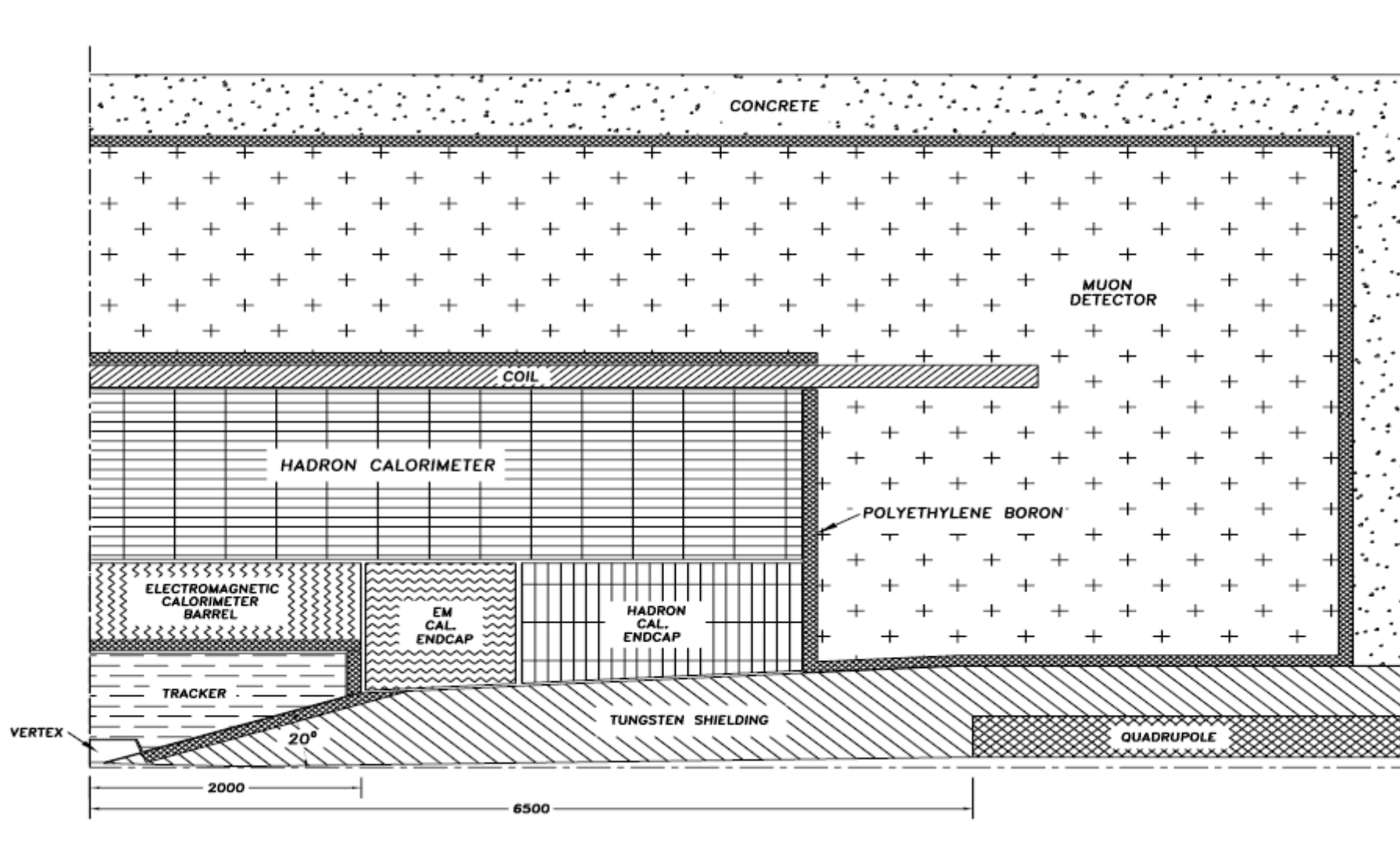
# Detector Shielding

- Work done in 96 for 2+2 TeV Collider (Iuliu Stumer)
- Solution was elaborate, but worked
- Needs to be redone for 1.5 TeV lattice



# Detector

- Detector was designed in 96 for 2+2 TeV
- Note forward 20 degrees is lost to detector

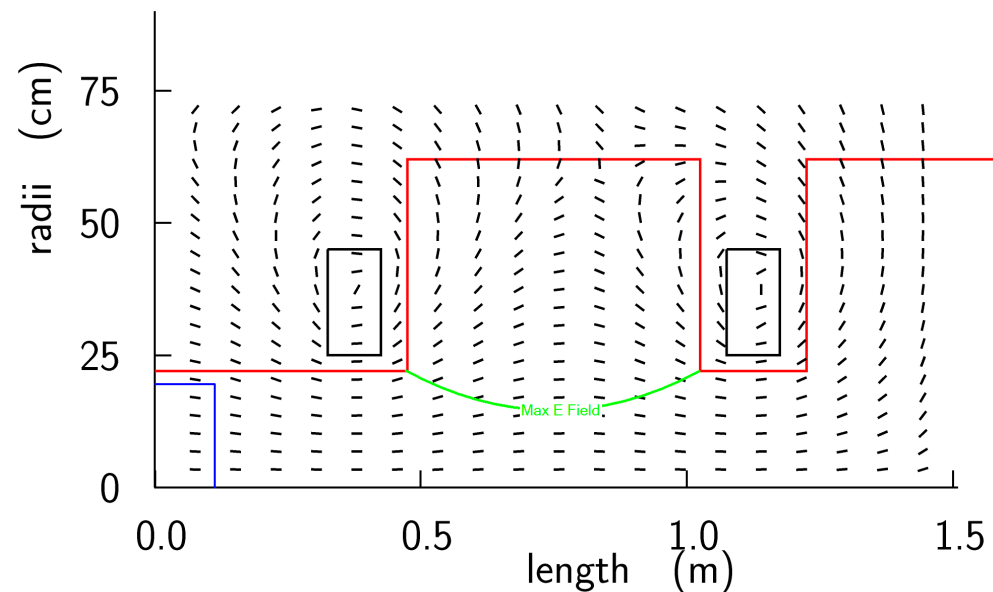
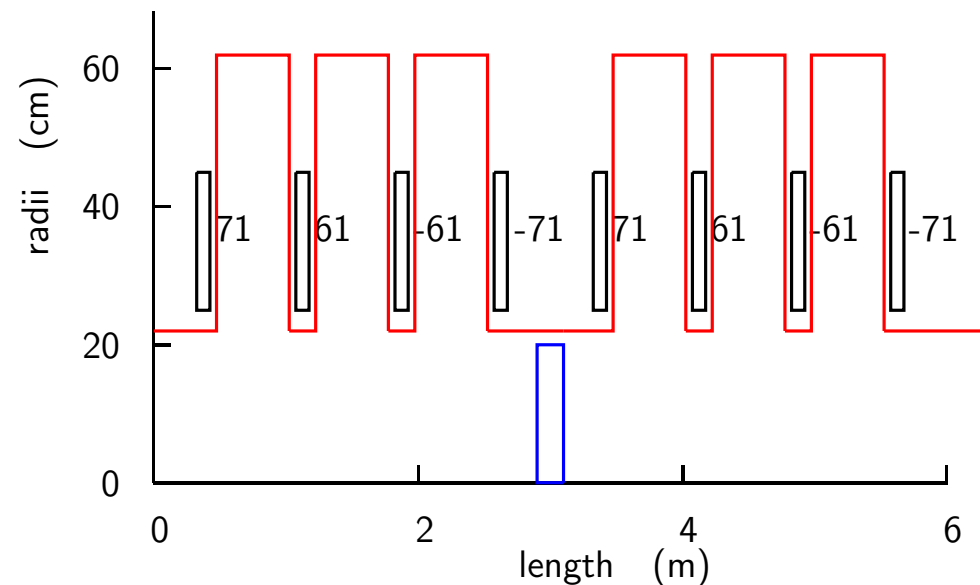
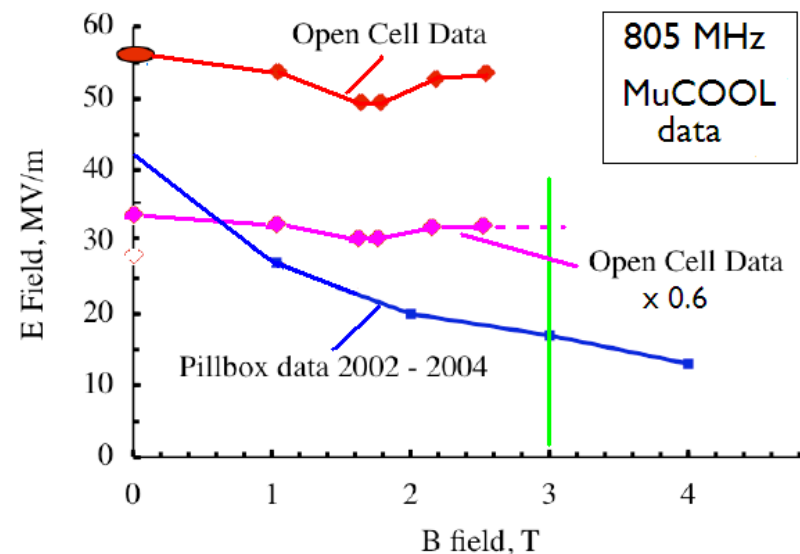


# Ongoing Studies

- Fuller simulations
- Space charge tune shifts (moderate, but not in simulations)
- Possible breakdown of vacuum RF in the specified magnetic fields
  - Being studied experimentally by MUCOOL Collaboration
  - Possible solution 1) Gas filled cavities  
works for earlier cooling lattices experiment needed for beam breakdown
  - Possible solution 2) Open Cavities with coils in irises (see next)  
works in simulation experiments needed for breakdown
- Planar wiggler lattice to replace Guggenheims (cools both muon signs)
- Fast Helical cooling in hydrogen gas  
Another alternative to RFOFO Guggenheims being studied by Muons Inc  
but difficult to introduce required rf
- Design of 50 T solenoids
- Use of more, but lower field (e.g. 35 T) final cooling solenoids
- Design detector shielding

# Open cell rf with coils in irises

- B field effect on open cavity much less  
average field/surface fields  $\approx 1/2$   
but open cavity still better at 3 T
- Should be even better if coils in irises
- Max E field  $\perp$  to B



# Conclusion

- New 1.5 TeV Collider lattice has more conservative IP parameters
  - Luminosity  $1 \times 10^{34}$  achieved with bunch rep rate  $\approx 12$  Hz
  - Collider ring must be deep (eg 135 m of ILC) to control neutrino radiation
  - Proton driver ( $\approx 4$  MW) is challenging
- Complete cooling scheme achieves required muon parameters
  - All components simulated (at some level) with realistic parameters
  - But much work remains
- Possible problem with rf breakdown in specified magnetic fields
  - Solutions with gas ?
  - Open cell rf ?
- Lower cost acceleration possible using pulsed magnets in synchrotrons
  - Rings fit in Tevatron tunnel
  - Second ring uses hybrid of fixed and pulsed magnets